



ANDHRA UNIVERSITY TRANS-DISCIPLINARY RESEARCH HUB

ADVANCED FLUID MECHANICS

UNIT I:

Non – viscous flow of incompressible Fluids: Lagrangian and Eulerian Descriptions of fluid motion- Path lines, Stream lines, Streak lines, stream tubes – velocity of a fluid particle, types of flows, Equations of three dimensional continuity equation- Stream and Velocity potential functions.

Basic Laws of fluid Flow: Condition for irrotationality, circulation & vorticity Acceleration in Cartesian systems normal and tangential accelerations, Euler's, Bernoulli equations in 3D – Continuity and Momentum Equations

UNIT 2:

Principles of Viscous Flow: Derivation of Navier-Stoke's Equations for viscous compressible flow – Exact solutions to certain simple cases: Plain Poiseuille flow - Couette flow with and without pressure gradient - Hagen Poiseuille flow - Blasius solution.

UNIT 3:

Boundary Layer Concepts: Prandtl's contribution to real fluid flows – Prandtl's boundary layer theory - Boundary layer thickness for flow over a flat plate – Approximate solutions – Creeping motion (Stokes) – Oseen's approximation - Von-Karman momentum integral equation for laminar boundary layer — Expressions for local and mean drag coefficients for different velocity profiles.

UNIT 4:

Introduction to Turbulent Flow: Fundamental concept of turbulence – Time Averaged Equations – Boundary Layer Equations - Prandtl Mixing Length Model - Universal Velocity Distribution Law: Van Driest Model – Approximate solutions for drag coefficients – More Refined Turbulence Models – k-epsilon model - boundary layer separation and form drag – Karman Vortex Trail, Boundary layer control, lift on circular cylinders

Internal Flow: Smooth and rough boundaries – Equations for Velocity Distribution and frictional Resistance in smooth through Pipes – Roughness of Commercial Pipes – Moody's diagram.

UNIT 5:

Compressible Fluid Flow – I: Thermodynamic basics – Equations of continuity, Momentum and Energy - Acoustic Velocity Derivation of Equation for Mach Number – Flow Regimes – Mach Angle – Mach Cone – Stagnation State

Compressible Fluid Flow – II: Area Variation, Property Relationships in terms of Mach number, Nozzles, Diffusers – Fanno and Releigh Lines, Property Relations – Isothermal Flow in Long Ducts –

Normal Compressible Shock, Oblique Shock: Expansion and Compressible Shocks – Supersonic Wave Drag.

TEXTBOOKS:

1. Schlichting H–Boundary Layer Theory (Springer Publications).
2. Convective Heat and Mass Transfer–Oosthigen, McGrawhill
3. Convective Heat and Mass Transfer–W.M.Kays, M.E.Crawford, McGrawhill

REFERENCEBOOKS:

1. Yuman S.W–Foundations of Fluid Mechanics.
2. An Introduction to Compressible Flow–Pai.
3. Dynamics & Theory and Dynamics of Compressible Fluid Flow –Shapiro.
4. Fluid Mechanics and Machinery–D.Rama Durgaiah.(New Age Pub.)
5. Fluid Dynamics–William F.Hughes & John A.Brighton (Tata McGraw-Hill Pub.)

MODEL QUESTION PAPER

ADVANCED FLUID MECHANICS

Time: 3 Hours

Max. Marks: 100

Answer Any **FIVE** questions only

All Questions Carry Equal Marks

- 1 a) Briefly explain the Lagrangian and Eulerian methods of describing fluid flows 10
b) Derive the three dimensional Bernoulli equation? 10
- 2 a) State the assumptions of Hagen-Poiseuille equation for laminar flow 5
b) Derive the Navier-Stokes Equations for viscous compressible flow. 15
- 3 a) The velocity distribution in the boundary layer is given by 10
$$\frac{u}{u_0} = \frac{3}{2} \left(\frac{y}{\delta}\right) - \frac{1}{2} \left(\frac{y}{\delta}\right)^3$$

determine the expressions for boundary layer thickness, wall shear stress and coefficient of drag in terms of Reynold's number

b) Derive the Von-Karman Integral momentum equation and reduce it to the case of flow over a flat plate 10
- 4 a) For turbulent flow in a pipe of 25 cm diameter, the centre line velocity is 2.25 m/s and the velocity at a point 8 cm from the centre as measured by a pitot tube is 1.95 m/s. Make calculations for (i) friction velocity and wall shearing stress, (ii) average velocity and discharge through the pipe, (iii) friction factor and (iv) pipe roughness. 15

b) Explain Turbulence Models? 5
- 5 a) A DC-10 aircraft cruises at 12 km altitude on a standard day. A pitot-static tube on the nose of the aircraft measures stagnation and static pressures of 29.6 kPa and 19.4 kPa.; Calculate (a) the flight Mach number of the aircraft, (b) the speed of the aircraft, and (c) the stagnation temperature that would be sensed by a probe on the aircraft 10

b) Discuss about the Fanno and Releigh Lines ? 10
- 6 a) A paddle wheel of 100mm diameter rotates at 150 rpm inside a closed concentric vertical cylinder of 300 mm diameter completely filled with a water. i. Assuming a 2D flow in a horizontal plane, find the difference in pressure between cylinder surface and the center of the wheel. ii. If provision is made for an outward radial flow which has a velocity of 1 m/s at the periphery of the wheel, what is the resultant velocity at a radius of 100 mm and its inclination to the radial direction? 10

b) The flow field of a fluid is given by 10
 $V = xyi + 2yzj - (yz + z^2)k,$
i. Show that it represents a possible 3-D steady incompressible continuous flow
ii. Is the flow is rotation or irrotational? iii. Angular velocity iv. Vorticity
- 7 a) A passage is designed to expand air isentropically to atmospheric pressure from a large tank in which properties are held constant at 5°C and 304 kPa (abs). The desired flow rate is 1 kg/s. Assuming the passage is 5 m long, and that the Mach number increases linearly with position in the passage, plot the cross-sectional 10

area and pressure as functions of position

b) A diffuser for an incompressible, inviscid fluid of density $\rho = 1000 \text{ kg/m}^3$ consists of a diverging section of pipe. At the inlet the diameter is $D = 0.25 \text{ m}$, and at the outlet the diameter is $D = 0.75 \text{ m}$. The diffuser length is $L = 1 \text{ m}$, and the diameter increases linearly with distance x along the diffuser. Derive and plot the acceleration of a fluid particle, assuming uniform flow at each section, if the speed at the inlet is $V = 5 \text{ m/s}$. Plot the pressure gradient through the diffuser, and find its maximum value. If the pressure gradient must be no greater than 25 kPa/m , how long would the diffuser have to be? 10

- 8 Explain the following: 20
- a. Moody's diagram
 - b. Plane Couette flow
 - c. Boundary layer separation
 - d. Creeping motion